

Semi-Analytic Model Predictions of the Galaxy Population in Proto-clusters

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ABSTRACT

We investigate the galaxy population in simulated proto-cluster regions using a semi-analytic model of galaxy formation, coupled to merger trees extracted from N-body simulations. We select the most massive clusters at redshift $z = 0$ from our set of simulations, and follow their main progenitors back in time. The analysis shows that proto-cluster regions are dominated by central galaxies and their number decreases with time as many become satellites, clustering around the central object. In agreement with observations, we find an increasing velocity dispersion with cosmic time, the increase being faster for satellites. The analysis shows that proto-clusters are very extended regions, $\gtrsim 20\text{ Mpc}$ at $z \gtrsim 1$. The fraction of galaxies in proto-cluster regions that are not progenitor of cluster galaxies varies with redshift, stellar mass and area considered. It is about 20-30 per cent for galaxies with stellar mass $\sim 10^9\text{ M}_\odot$, while negligible for the most massive galaxies considered. Nevertheless, these objects have properties similar to those of progenitors. We investigate the building-up of the passive-sequence in clusters, and find that their progenitors are on average always active at any redshift of interest of proto-clusters. The main mechanism which quenches their star formation is the removal of the hot gas reservoir at the time of accretion. The later galaxies are accreted (become satellite), and the more the cold gas available, the longer the time spent as active. Central galaxies are active over all redshift range considered, although a non-negligible fraction of them become passive at redshift $z < 1$, due to strong feedback from Active Galactic Nuclei.

Key words: clusters: general - galaxies: evolution - galaxy: formation.

1 INTRODUCTION

The term ‘proto-cluster’ is used to refer to the over-density regions in the early Universe that are believed to evolve into massive galaxy clusters today. Putative proto-cluster regions were often localized around high- z radio galaxies (HzRGs, e.g., Pentericci et al. 1997; Miley et al. 2004; Kurk et al. 2004; Venemans et al. 2007; Kuiper et al. 2011), that are among the most massive galaxies at high redshift, and likely the progenitors of massive elliptical galaxies residing at the centre of local massive clusters (e.g., McLure et al. 1999; Zirm et al. 2005; Cooke et al. 2008; Miley & De Breuck 2008; Hatch et al. 2011). Proto-cluster galaxies can be efficiently identified using narrow-band

imaging to detect emission line ($\text{Ly}\alpha$ or $\text{H}\alpha$) objects at the redshift of the target HzRG. Alternatively, broad-band imaging can be used, with colours chosen to detect dropout objects at the target redshift. Follow-up spectroscopy is then needed to confirm the redshift of the candidate proto-cluster galaxies. Being proto-clusters regions of intense star formation activity, efficient searches can be conducted using the far-IR/submm bands. Recently, Clements et al. (2014) exploited the all sky coverage of the Planck satellite survey in combination with Herschel data, in order to detect candidate clusters undergoing dust-obscured violent star forming phase (see also Planck Collaboration et al. 2015).

While, for practical reasons, observational studies are often based on relatively small areas around putative sign-posts of proto-clusters (e.g. Venemans et al. 2007; Hatch et al. 2009), it has been soon realized that these struc-

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tures cover extended regions, up to 20 Mpc (Kurk et al. 2004; Tanaka et al. 2011; Hatch et al. 2011; Toshikawa et al. 2012). Therefore, large areas are needed if the goal is to probe a large fraction of the proto-cluster galaxy population.

From the theoretical viewpoint, a few recent studies have compared observational data with results from theoretical models of galaxy formation or used such models to interpret the observational results. Saro et al. (2009) compared results from hydrodynamical simulations of galaxy clusters to the observational properties of the Spiderweb galaxy system. Similar comparison work has been carried out more recently by Granato et al. (2015), who pointed out that simulated cluster regions never reach the elevated star formation rates inferred from observational studies of proto-cluster regions. Overzier et al. (2009) used mock catalogues based on semi-analytic models of galaxy formation applied to the Millennium Simulation to study the relation between density enhancements around QSOs and proto-cluster regions at $z \sim 6$. More recently, Chiang et al. (2013), Orsi et al. (2015), and Muldrew et al. (2015) used similar techniques to study the relation between proto-clusters identified using common observational techniques and present day cluster descendants, and that between high redshift clusters and proto-clusters.

In this work, we adopt a similar approach and focus on the characterization of the size and ‘contamination’ from non cluster galaxies of proto-cluster regions, star formation activity within the proto-clusters, and origin of the passive sequence observed in local galaxy clusters.

The paper is structured as follows: in Section 2 we present our set of simulations and the sample of proto-cluster regions. Results from our case study are discussed in Section 3, where we analyse the spatial distribution of central and satellites galaxies in proto-clusters, their velocity dispersion and total star formation rate. The latter will be discussed in detail in Section 6 by using the full sample of proto-cluster regions. In Section 4 we quantify the fraction of progenitors in boxes centred around the central galaxy with different sizes, to statistically characterize the typical size of proto-cluster regions. In Section 5 we focus on the fraction of outliers (defined as those objects that are not progenitors of galaxies in cluster at $z = 0$) in proto-clusters as a function of galaxy stellar mass and redshift, while in Section 7 we follow the history of the proto-cluster galaxy population, focusing mainly on the progenitors of passive galaxies at $z = 0$. Finally, we discuss our results and give our conclusions in Section 8.

2 THE SIMULATED CLUSTERS

In this study we use N-body simulations of galaxy clusters, generated using the ‘zoom’ technique (Tormen, Bouchet & White 1997, see also Katz & White 1993): a target cluster is selected from a parent low-resolution simulation of a large cosmological volume and all its particles, as well as those in its immediate surroundings, are traced back to their Lagrangian region and replaced with a larger number of lower mass particles. Outside this high-resolution region, particles of increasing mass are displaced on a spherical grid. All particles are then

perturbed using the same fluctuation field used in the parent cosmological simulations, but now extended to smaller scales. The method allows the computational effort to be concentrated on the cluster of interest, while maintaining a faithful representation of the large scale density and velocity. All the cluster re-simulations used in this study are based on the same parent simulation. This followed 1024^3 dark matter particles within a box of $1h^{-1}\text{ Gpc}$ comoving on a side.

Below, we use cosmological N-body simulations of 27 regions surrounding as many massive clusters identified at $z=0$, and carried out assuming the following cosmological parameters: $\Omega_m = 0.24$ for the matter density parameter, $\Omega_{\text{bar}} = 0.04$ for the contribution of baryons, $H_0 = 72\text{ km s}^{-1}\text{Mpc}^{-1}$ for the present-day Hubble constant, $n_s = 0.96$ for the primordial spectral index, and $\sigma_8 = 0.8$ for the normalization of the power spectrum. The latter is expressed as the r.m.s. fluctuation level at $z = 0$, within a top-hat sphere of $8h^{-1}\text{Mpc}$ radius. For all simulations, the mass of each dark matter particle in the high resolution region is $10^8 h^{-1}M_\odot$, and the Plummer-equivalent softening length is fixed to $\epsilon = 2.3h^{-1}\text{ kpc}$ in physical units at $z < 2$, and in comoving units at higher redshift.

For each simulation, outputs have been stored at 93 redshifts, between $z = 60$ and $z = 0$. Dark matter haloes have been identified using a standard friends-of-friends (FOF) algorithm, with a linking length of 0.16 in units of the mean inter-particle separation in the high-resolution region. The algorithm SUBFIND (Springel et al. 2001) has then been used to decompose each FOF group into a set of disjoint substructures, identified as locally overdense regions in the density field of the background halo. Only substructures that retain at least 20 bound particles after a gravitational unbinding procedure are retained as genuine substructures. Finally, merger histories have been constructed for all self-bound structures in our simulations, using the same post-processing algorithm that has been employed for the Millennium Simulation (Springel et al. 2005). For more details on the simulations, as well as on their post-processing, we refer the reader to Contini et al. (2012). For our analysis, we use a sample of 27 haloes, extracted from the high resolution regions of these simulations, and with mass larger than $\sim 5 \cdot 10^{14} h^{-1}M_\odot$. In particular, 5 of our simulated haloes have $M_{200} \sim 10^{14}M_\odot$, 9 $M_{200} \sim 7 - 8 \cdot 10^{14}M_\odot$ and the remaining 13 $M_{200} \sim 10^{15}M_\odot$.

We make use of the merger-trees extracted from our set of simulated clusters to construct a mock catalogue of proto-cluster regions. The evolution of the galaxy population is described by a semi-analytic model that is based on a modified version of that presented in De Lucia & Blaizot (2007). In particular, we use the updates presented in Contini et al. (2014), that include an explicit modelling for the formation of the intra-cluster light (ICL) via stripping processes and mergers. We use the combination *Model Tidal Radius+Mergers* presented in that paper, but we stress that the results presented below are not affected by the particular model used for the formation of the ICL. The updated model introduced in Contini et al. (2014) adopts the same parameter set used by the original model described in De Lucia & Blaizot (2007). The model was originally calibrated to match primarily the local K-band luminosity func-

tion. No high redshift data was used to tune the model parameters.

We run the semi-analytic model on the merger-trees extracted from the simulations and generate galaxy-trees, i.e. catalogues that contain, for each model galaxy, information about all its progenitors and descendants. We then select all galaxies within the virial radius R_{200} of each simulated cluster, and for each of them, we follow its tree by considering all progenitors with stellar mass larger than $2 \cdot 10^8 M_\odot$ (this roughly corresponds to our resolution limit). At each redshift, we consider the region occupied by all progenitors of $z = 0$ cluster galaxies as the proto-cluster region, i.e. the boundaries of the proto-cluster regions are given by the distribution of progenitors they contain. The center of each region is defined by the position of the main progenitor of the central object found at redshift $z = 0$. For the analysis that follows, unless otherwise stated, scale-lengths are given in comoving units.

In the following analysis, we have avoided including galaxies from the low-resolution regions of each re-simulation. To this aim, when the analysis requires the selection of galaxies within some distance from the central galaxy, we have only considered galaxies in cubic regions of $\sim 7 h^{-1} \text{Mpc}$ on a side for the 5 clusters in our sample with mass $\sim 10^{14} h^{-1} M_\odot$. These 5 clusters are not included in some analysis considering larger regions of the proto-clusters (e.g. Figs. 4 and 6 below). For all other simulated clusters, the high-resolution regions extends at least out to $\sim 15 h^{-1} \text{Mpc}$.

3 THE ORIGIN OF A MASSIVE CLUSTER

In this section, we analyse in detail the proto-cluster region corresponding to our most massive ($M_{200} \sim 10^{15} h^{-1} M_\odot$) galaxy cluster at $z = 0$. In Figure 1, we show the x-y projections of progenitor positions at four different redshifts: $z = 0.60, 1.00, 1.61, 3.02$. Satellite galaxies are plotted in red, while centrals are in blue. The black circle in each panel indicates a multiple of the virial radius (as indicated in the legend) of the halo that contains the central galaxy (CG, hereafter). The latter is identified as the central galaxy in the main progenitor of the final cluster at each redshift.

Figure 1 shows that our most massive proto-cluster region is dominated by central galaxies at high redshifts (see also Diener et al. 2015), and that their number decreases with decreasing redshift. At redshift $z = 0.60$, most of the centrals have become satellites and entered the innermost regions of the proto-cluster. As we will see below, central galaxies are typically star-forming systems at high-redshift. The fraction of central galaxies that we find at high redshift (~ 0.7) is consistent with recent results by Hatch et al. (2011), who find that 77 ± 10 per cent of galaxies in a sample of proto-clusters at $2.2 < z < 2.6$ are blue. In our model, most of the satellites are passive while centrals (excluded the most massive ones) are typically active. At this redshift, we find that about 80 per cent of the galaxies in the proto-cluster regions have specific star formation rate higher than

10^{-11}yr^{-1} . The comparison with results by Hatch et al. (2011) is just qualitative at this stage. Their fraction is based on a sample of galaxies centred around 6 HzRGs and within a radius of 3.5 comoving Mpc, with redshifts between 2.28 and 2.55 from the collection of Miley & De Breuck (2008). We will come back to this issue below.

The CG grows by a factor four in stellar mass between $z \sim 3$ and $z \sim 1$, and then by a factor 2-3 between $z \sim 1$ and the present time (De Lucia & Blaizot 2007; Contini et al. 2014). The growth of the CG is mainly driven by accretion of lower mass galaxies with the region around the CG not containing many galaxies with comparable stellar mass over the redshift range considered. Hatch et al. (2009) studied the stellar mass assembly of MRC 1138-262, also known as the Spiderweb Galaxy, a massive radio galaxy in a proto-cluster region at $z = 2.2$. They identify the galaxies at the same redshift and within a projected distance of 150 kpc from the radio galaxy. Assuming that these satellites all lie on circular orbits around the radio galaxy, with radii given by their projected radii, they estimate their merging time-scale analytically (see their Eq. 3), and predict that most of them will merge with the central radio galaxy before $z = 0$ increasing their mass by up to a factor 2. In our test case, we find that 95 per cent of the satellites within 150 kpc from the central galaxy will merge with it by $z = 0$, in agreement with the calculation by Hatch et al.

In Figure 2, we show maps of the velocity field at the four redshifts considered for Fig. 1. Arrows indicate the direction of the motion, and are colour coded accordingly to the velocity modulus. Positions and velocities have been normalized to the CG position and velocity at each redshift. At high redshifts, progenitors have, on average, low velocities with respect to the CG. This is because the halo potential is not very deep and the progenitors are still relatively far away from it. The velocities tend to increase towards $z = 0$, as progenitors approach the central regions of the cluster main progenitor. The halo potential also becomes deeper with decreasing redshift as the cluster grows in mass.

In Figure 3, we plot the velocity distribution of central (dashed lines), satellite (dash-dotted lines), and all progenitor galaxies (solid lines) at the same redshifts of figures 1 and 2. The figure clearly shows that the velocity distribution of centrals and satellites widen approaching the present time, i.e. the velocity dispersion increases with cosmic time, in good agreement with observations (e.g., Venemans et al. 2007)¹.

In Table 1 we list the velocity dispersions of centrals, satellites and all progenitor galaxies, at the four redshifts considered. We see that the velocity dispersions of satellites and centrals are similar at high- z , but that of satellites increases faster, becoming larger than the velocity dispersion of centrals at low redshift. This is because galaxies grow in mass as centrals and then join the densest regions as satellites. As haloes grow in mass, the velocity dispersion of satellites within them increases.

¹ We note that our velocity dispersions have been calculated using dynamical information provided by the simulation, while observationally they are determined using redshift information, and are typically based on a few proto-cluster members over relatively limited regions

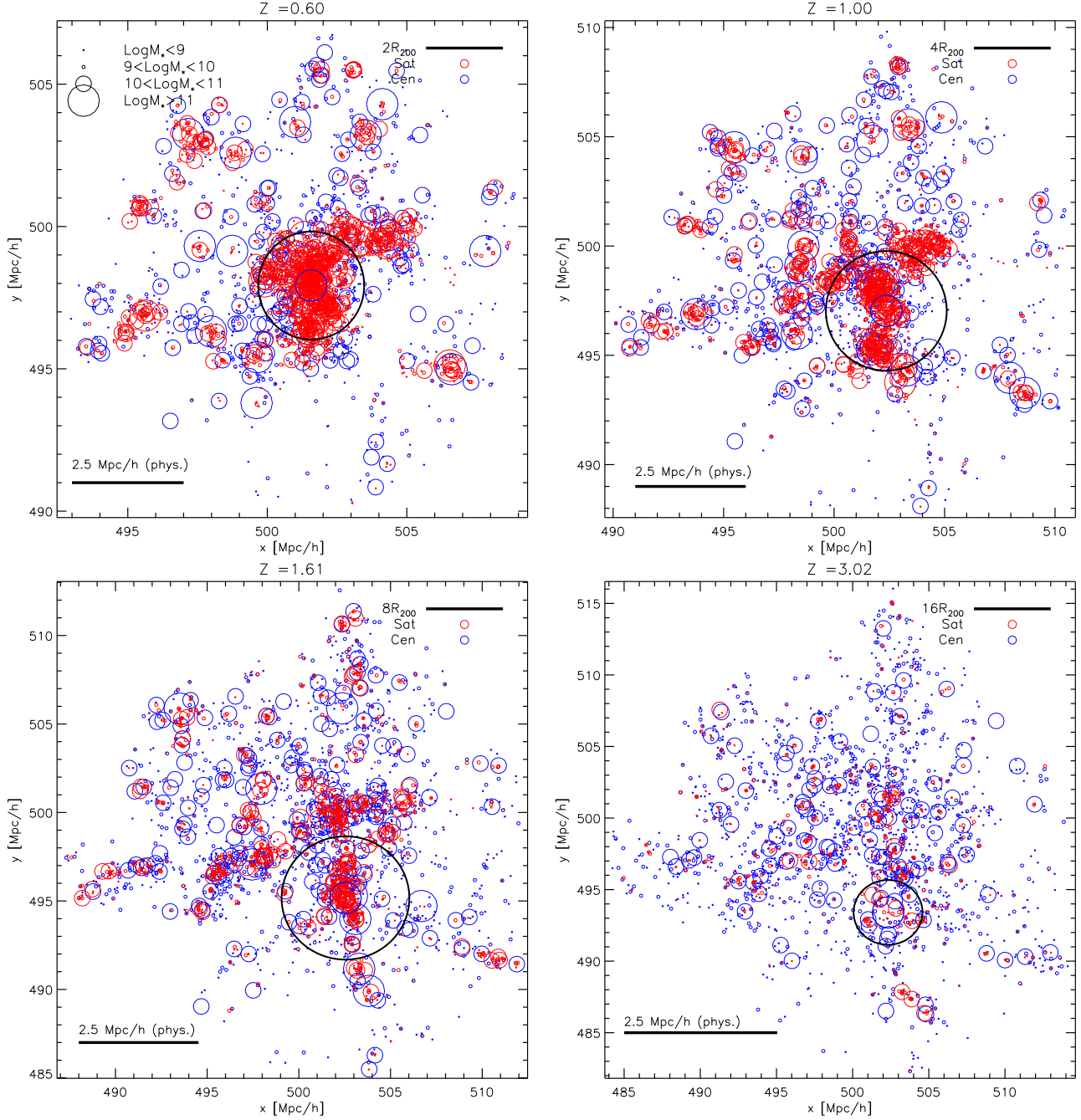


Figure 1. X-Y positions of all progenitors of galaxies residing within R_{200} of the most massive cluster in our sample at $z = 0$. Progenitor distributions are plotted at four different redshifts, with red circles marking satellite galaxies and blue circles marking central galaxies. The dimension of each circle is proportional to the stellar mass of the galaxy. The black circle in each panel show a multiple of the virial radius of the halo containing the central galaxy at each z . The latter is identified as the galaxy sitting at the centre of the most massive cluster progenitor at each redshift.

Results presented above show that the proto-cluster region of the most massive cluster in our sample is very extended, $\sim 20 h^{-1} \text{Mpc}$, and hosts mainly a population of central galaxies at high redshift. At this redshift, central galaxies are actively forming stars so that the proto-cluster is a region of intense star formation. For the particular example shown in this section, our model predicts a total star formation rate of about $500 M_{\odot}/\text{yr}$ in the very inner region and at $z \sim 2.6$.

4 FRACTION OF PROGENITORS IN PROTO-CLUSTER REGIONS

The results discussed in the previous section confirm that proto-clusters are extended objects, and that their size clearly depends on the particular redshift at which they are observed. In this section, we focus on the characterization of the typical size of proto-cluster regions by quantifying the fraction of progenitors in regions of different comoving size.

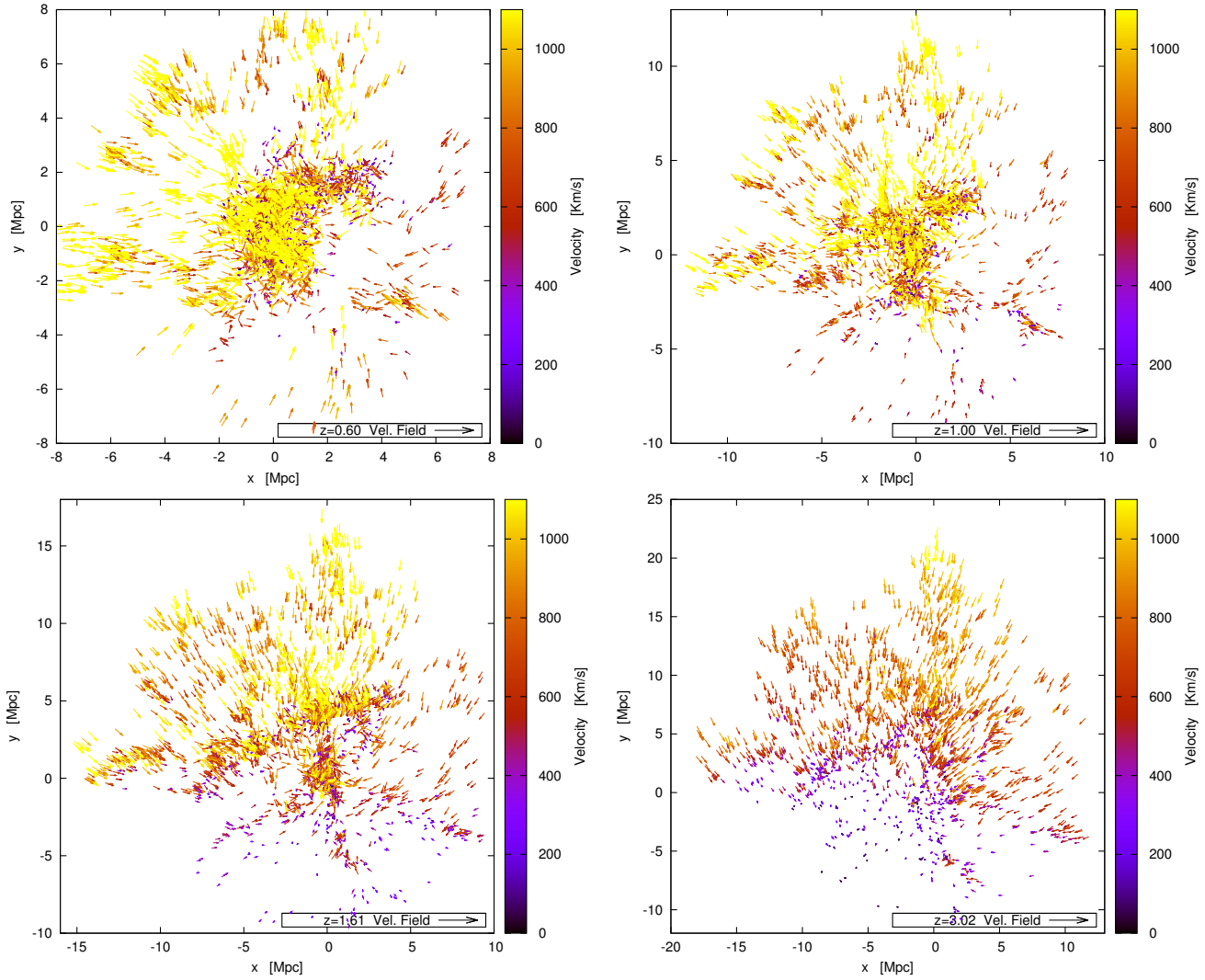


Figure 2. Velocity field of all progenitors of galaxies in the most massive cluster in our sample, at the same redshifts considered in Fig. 1. Positions and velocities have been computed using all three components for each model galaxy, and shifting them with respect to those of the CG, at each redshift. Arrows indicate the direction of the motion while the modulus is given by the colour coding.

Table 1. Velocity dispersions for the three samples of galaxies used in Figure 3 at the four different redshifts considered. Units are km/s and velocities have been normalized to the CG velocity.

Sample	$z=0.60$	$z=1.00$	$z=1.61$	$z=3.02$
All	432	355	309	250
Centrals	330	286	283	247
Satellites	460	391	335	258

The number of systems in our sample (27) allows us to provide also an estimate of the halo-to-halo scatter. Our results do not depend significantly on the mass of the final cluster and, therefore, we discuss the average trend of our complete sample. In a recent study, Chiang et al. (2013) find a tight correlation between the size of the proto-cluster and the cluster final mass, which appears in contradiction with our previous statement. We note, however, that Chiang et al. (2013) identify proto-clusters using a different method and consider

a larger dynamical range in the mass of the final cluster. In line with our results are those by Orsi et al. (2015), who provide a prediction for the evolution of a typical size of proto-clusters with redshift that does not depend significantly on final cluster mass.

In the left panel of Figure 4 we plot the ratio between the number of progenitors contained in cubic boxes of different sizes ($5, 10, 15 h^{-1} Mpc$) centred around the CG at each redshift, and the total number of progenitors with stellar mass above $10^9 M_\odot$ (we do not find significant differences using higher cuts in stellar mass) as a function of the proto-cluster redshift. Solid lines show the median fractions, while shaded regions mark the 20th-80th percentiles area. Proto-clusters are often identified around high- z ($z \gtrsim 1.5$) radio galaxies, considering areas of few Mpc^2 (typically less than $2 \times 2 Mpc$ physical) around the radio galaxy. Over the same redshift range, for the proto-clusters considered in our study, the fraction of progenitors varies between 0.2 to almost zero if computed in a box of $5 h^{-1} Mpc$ (blue solid line and shaded area), and between 0.6 to 0.4 within a box of $15 h^{-1} Mpc$

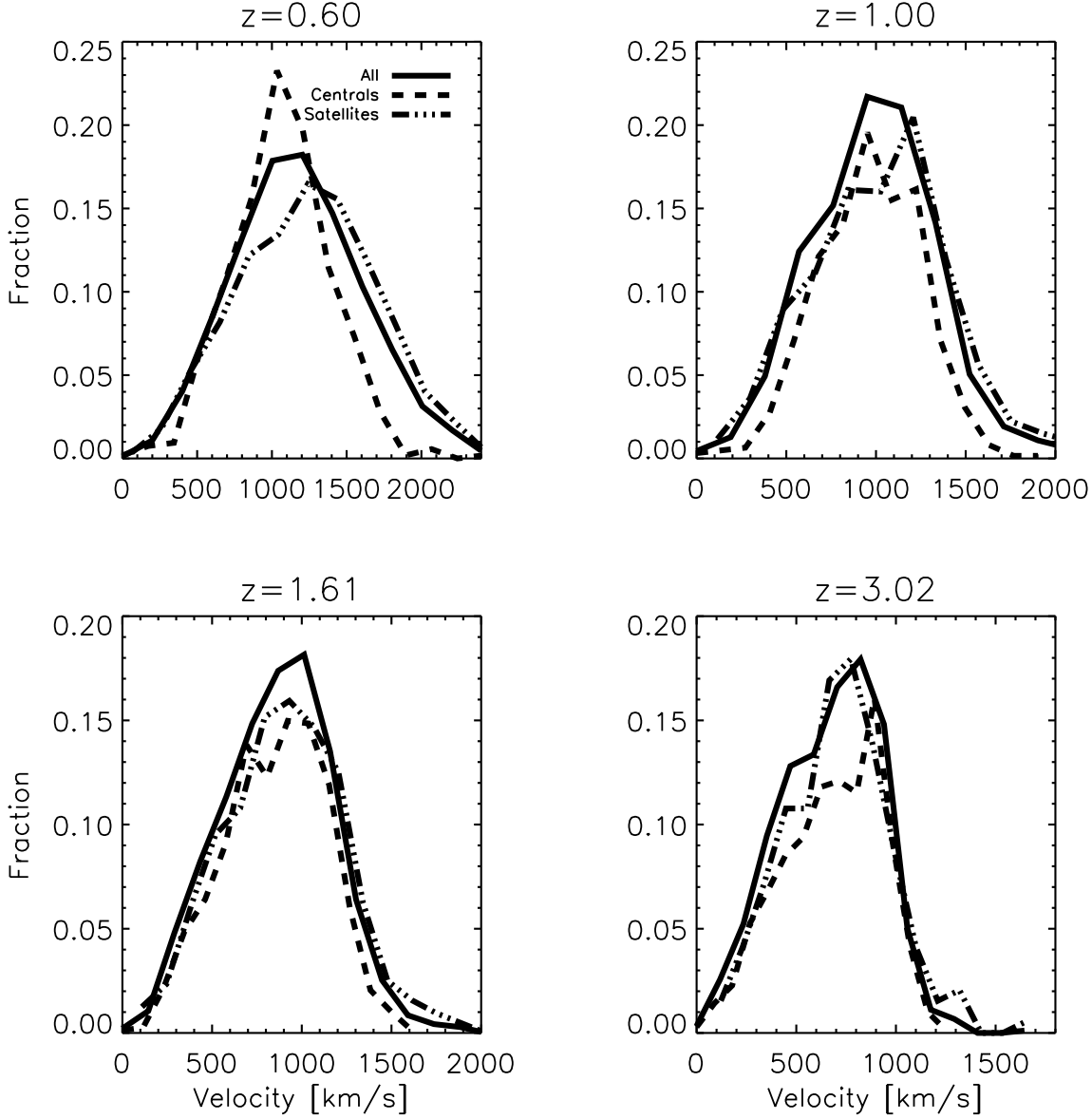


Figure 3. Velocity distribution for all (solid lines), central (dashed lines) and satellite (dash-dotted lines) progenitor galaxies, at the same redshifts considered in Figures 1 and 2. Velocities have been computed using all three velocity components for each model galaxy, and shifting them with respect to those of the CG, at each redshift.

(green solid line and shaded area). Therefore, as stressed above, very large regions are needed in order to include the bulk of the galaxy population in proto-clusters at high redshift.

The right panel of Figure 4 shows the same quantities given in the left panel, but now considering the geometrical centre of the proto-cluster region, defined by the median x , y , and z of all proto-cluster galaxies. The fractions corresponding to the 10 and $15 h^{-1} Mpc$ boxes are similar to those plotted in the left panel. For the smallest box considered, the fractions computed around the CG are about twice those computed using the geometrical centre for $z > 2$. Therefore, the distribution of progenitors in the sky is not typically symmetric around the CG.

In Figure 5, we plot the median CG distance from the geometrical centre (solid line) of the proto-cluster region as a

function of redshift. Dashed lines indicate the 10th and 90th percentiles of the distributions. The shift between the CG position and the geometrical centre is always larger than $\sim 2 h^{-1} Mpc$. It becomes $\sim 5 h^{-1} Mpc$ at $z \sim 2$, and $\sim 6 h^{-1} Mpc$ at $z \sim 3$. This is due in part to the high number of progenitors residing in haloes that have not yet merged with the main progenitor of the final cluster. In addition, the bulk motion of progenitors, as seen in Figure 3, causes a decrease with decreasing redshift of the shift.

5 OUTLIERS IN PROTO-CLUSTER REGIONS

As mentioned above, proto-cluster regions are often identified around luminous galaxies at high redshifts. Our simulated catalogues allow us to estimate what is the typical

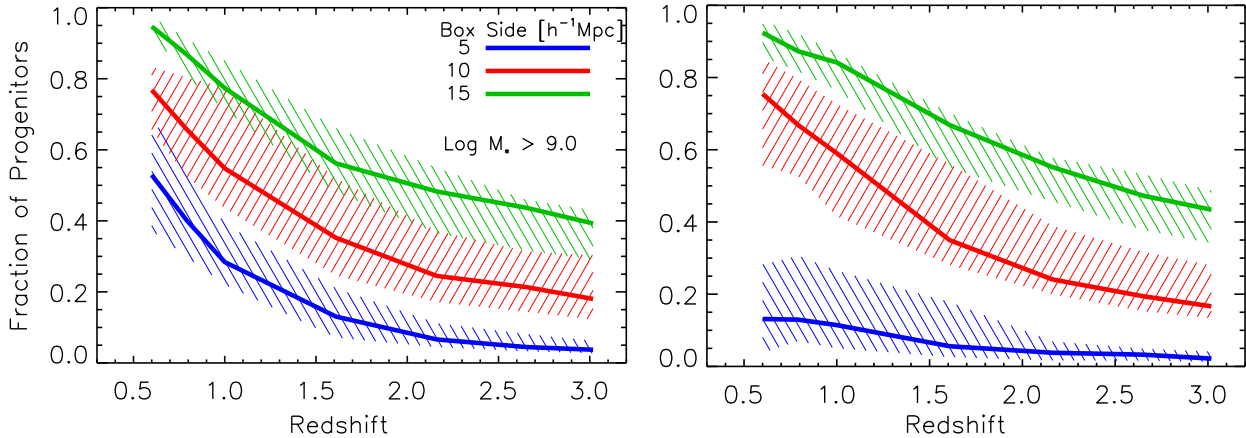


Figure 4. Left panel: ratio between the number of progenitors contained in cubic boxes of different sizes (5, 10, 15 $h^{-1}Mpc$) centred around the CG at each redshift, and the total number of progenitors in the proto-cluster region (including those outside the box) with stellar mass above $10^9 M_{\odot}$, as a function of redshift. Solid lines represent the median relations, while shaded regions mark the 20th-80th percentiles. Fractions have been computed by considering the CG position as the centre at each redshift. Right panel: same as left panel, but computing fractions by considering the geometrical centre (median x, y, z of all proto-cluster galaxies at each redshift).

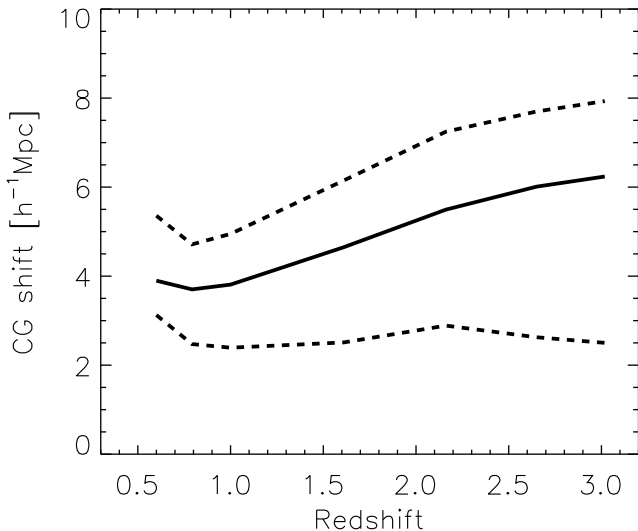


Figure 5. Shift of the CG with respect to the geometrical centre of the proto-cluster region, as defined in Figure 4. Solid lines represent the median, while dashed lines represent the 10th and 90th percentiles of the distribution.

fraction of ‘outliers’, i.e. of galaxies in the region that are not actual progenitors of a galaxy residing in the descendant cluster at $z = 0$. In particular, we will consider ‘outliers’ all galaxies that are not progenitors of cluster galaxies located within $2 \cdot R_{200}$ of the cluster at $z = 0$.

In Figure 6 we plot the fraction of actual progenitors in our proto-cluster regions within cubic boxes of different sizes (5 for all 27 regions considered in this study, and 10, 15 $h^{-1}Mpc$ for the 22 regions corresponding to the 22 most massive clusters at $z = 0$) centred around the CG, as a function of their stellar mass, and at four different redshifts. Solid lines represent the median fractions, while shaded areas represent the distribution between the 20th and 80th percentiles. This scatter is larger at increasing redshift, irrespective of the size of the box. The plot shows that the

fraction of actual progenitors weakly increases with progenitor stellar mass, between 0.6 for progenitors with stellar mass around $M_* \sim 10^9 M_{\odot}$, and 1 for stellar masses of about $10^{11} M_{\odot}$ at $z \gtrsim 2$. The trend is analogous at lower redshift, but the fraction is higher at low stellar mass. The fraction at high stellar mass and at high redshift is affected by low-number statistics.

Our analysis shows that, in our simulated proto-cluster regions, the fraction of outliers depends on the galaxy stellar mass and (weakly) on the redshift at which proto-cluster regions are located, and does not strongly depend on the size of the box up to 15 comoving Mpc. We find that about 30 per cent of galaxies with stellar mass smaller than $\sim 10^{10} M_{\odot}$ are outliers at $z \sim 3$, and that this fraction rapidly decreases towards larger stellar mass. Slightly smaller fractions are found at lower redshifts, and when considering progenitors of galaxies within R_{200} (instead of $2 \cdot R_{200}$) at redshift zero.

Our analysis also shows that it is virtually impossible to distinguish between outliers and actual progenitors by looking at their physical properties: we have verified that the distribution of colours, star formation rates, cold, hot and stellar masses or location in the proto-cluster regions for outliers do not differ significantly from those of progenitors. We have verified that the proto-cluster members and outliers also share similar line-of-sight velocity distributions. However, it is worth noting that this set of simulations is not ideal for addressing this issue. In fact, the high-resolution region of our cluster re-simulations only allow us to consider regions of the Universe corresponding to the surroundings of massive clusters. Therefore, these outliers may not be representative of the average ‘field’ galaxy.

Finally, we stress that we do not mimic exactly the typical observational procedure that is adopted to select proto-cluster galaxy candidates. This would require the construction of light-cones and the application of similar selection procedures as done by other authors (e.g. Overzier et al. 2008.) However, our results indicate that even with very high spectral resolution observations, we will be unable to

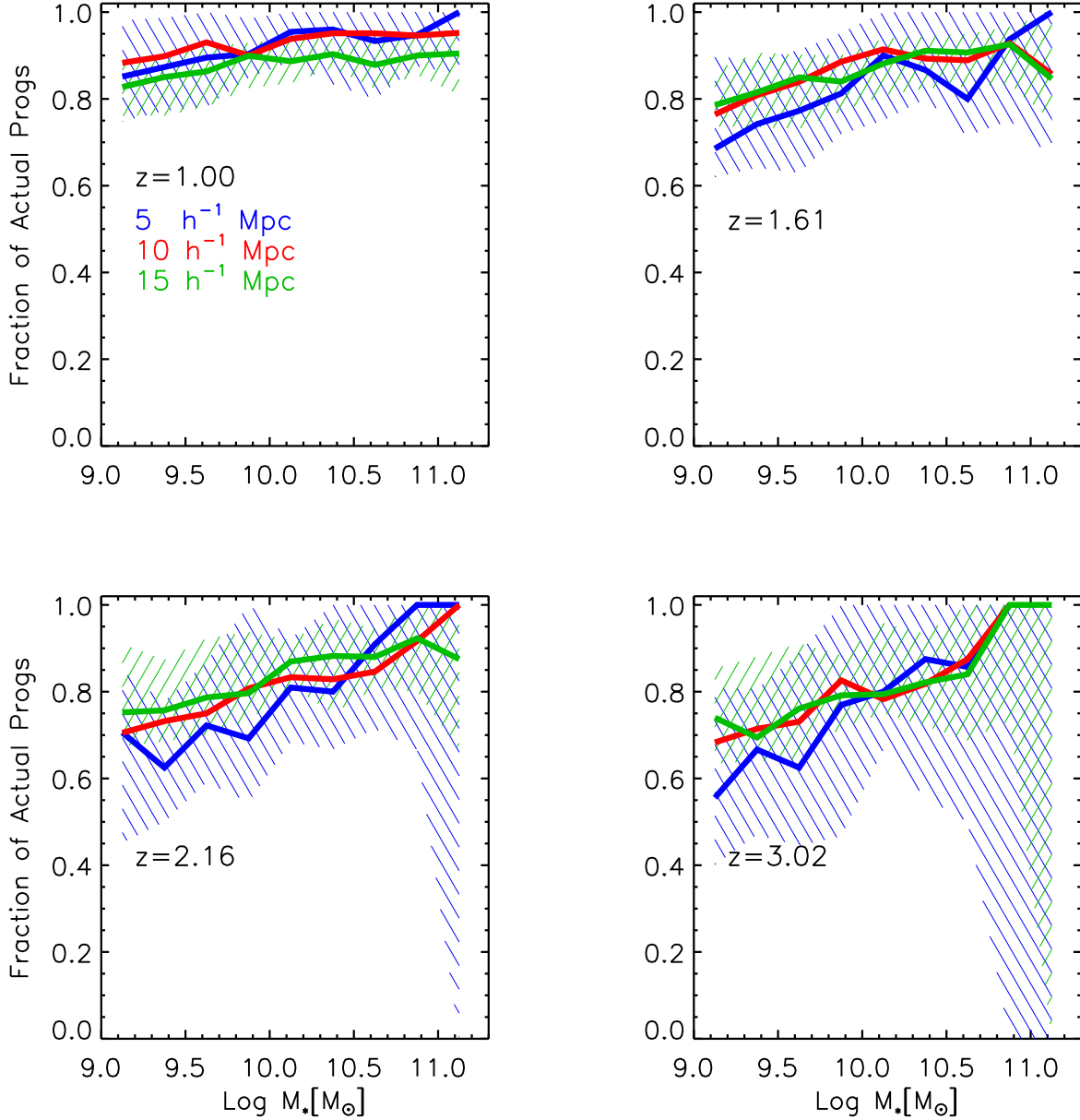


Figure 6. Fraction of actual progenitors in our simulated proto-cluster regions within cubic boxes of different sizes as indicated in the legend, as a function of stellar mass and at different redshifts. Solid lines represent the median, while shaded areas show the distribution between the 20th and 80th percentiles for the smallest and largest boxes. The scatter around the red solid lines is comparable to that corresponding to the largest box size.

distinguish outliers from true proto-cluster galaxies as they occupy the same volume.

6 STAR FORMATION RATE IN PROTO-CLUSTERS

Proto-clusters are regions of strong star formation activity (Pentericci et al. 2001; Miley et al. 2006; Overzier et al. 2008; Hatch et al. 2008, 2011; Tanaka et al. 2011; Hayashi et al. 2012). Tanaka et al. (2011) report the discovery of a significant excess, about a factor 5 with respect to the field, of candidate $H\alpha$ emitters in the proto-cluster associated with the radio galaxy 4C 23.56 at

$z = 2.48$. Combined with mid-infrared photometric data, they conclude that active star formation must be occurring in the proto-cluster region around the radio galaxy, and that its rate should be comparable with that of the average field at the same redshift. Hatch et al. (2011), who investigate the proto-clusters surrounding MRC 1138-262, at $z \sim 2.2$, and 4C + 10.48, at $z \sim 2.35$, find a total star formation rate within the central 1.5 Mpc of about $5000 M_{\odot}/\text{yr}$ for the former, and about $3000 M_{\odot}/\text{yr}$ for the latter, much higher than the typical star formation rate in local galaxy clusters (Koyama et al. 2010; Wetzel et al. 2012, and references therein). Hayashi et al. (2012), however, find smaller total star formation rates in three clumps (two of which corre-

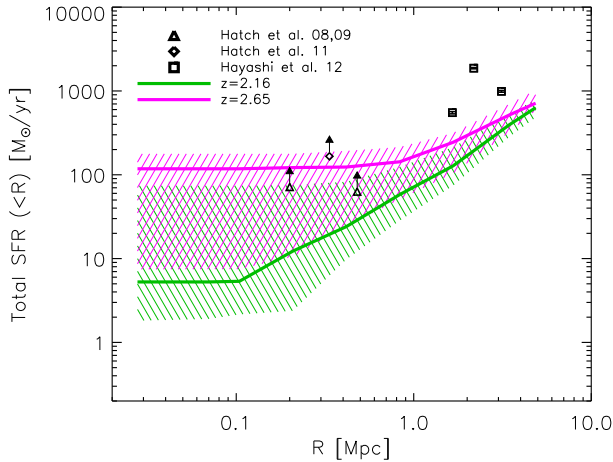


Figure 7. Total star formation rate (cumulative) of galaxies in the proto-cluster regions as a function of the projected distance from the centre, at different redshifts (lines of different colours). Solid lines represent the median value calculated on the 27 proto-cluster regions, and shaded areas represent the distribution between the 20th and 80th percentiles. Black triangles and diamond represent the observational data by Hatch et al. (2008 2009), and Hatch et al. (2011), respectively, and black squares represent observational measurements by Hayashi et al. (2012).

sponding to areas larger than 4.5 Mpc^2) around the radio galaxy USS 1558-003 at redshift $z = 2.53$. In the central region $50 \times 40 \text{ kpc}$ of MRC 1138-262, Miley et al. (2006) find a total star formation rate $\gtrsim 100 M_\odot/\text{yr}$, in good agreement with the total star formation rate, $130 \pm 13 M_\odot/\text{yr}$, that Hatch et al. (2008) obtain in the central region $65 \times 65 \text{ kpc}$ of the same object. A similar amount of star formation ($302 M_\odot/\text{yr}$) is found by Hatch et al. (2011) in the central region, $100 \times 100 \text{ kpc}$, of $4C + 10.48$. Very high ‘total’ star formation rates ($\sim 10^4 M_\odot/\text{yr}$) have been measured recently by Clements et al. (2014) for overdensities of Herschel sources.

In Figure 7 we show the total star formation rate of galaxies in our proto-cluster regions within an area of size plotted on the x-axis, at different redshifts (lines of different colours). Solid lines represent the median value, while shaded areas represent the distribution between the 20th and 80th percentiles. The total star formation rate of galaxies within a given area of our proto-cluster regions is a decreasing function of redshift, in qualitative agreement with observations. Quantitatively, however, our model predictions are offset with respect to the observational data. In particular, the observational data by Hatch et al. (2008) and Hatch et al. (2009) (black triangles) should be compared with the green line, while Hatch et al. (2011) (black diamond), and Hayashi et al. 2012 (squares) should lie between the green and magenta lines.

All these studies (but Hatch et al. 2009) use a Salpeter IMF (Salpeter 1955), while our model (as Hatch et al. 2009) adopts a Chabrier (Chabrier 2003) initial mass function (IMF). Following Longhetti & Saracco (2009), we have corrected star formation rate estimates based on the assumption of a Salpeter IMF, using the following conversion

$$SFR_{\text{Cha}}(z) = 0.55 \cdot SFR_{\text{Sal}}(z).$$

We also note that the observational estimates are dust-uncorrected. Assuming a minimum of dust extinction, especially in the inner regions, they move up to the upper limits of our predictions, even beyond $100 M_\odot/\text{yr}$. Hence, despite the large object-to-object scatter especially at high redshift and in the inner regions, our model predicts star formation rates that are lower than observational estimates by a factor of 2 in the innermost regions and up to a factor of 5 or so at larger radii. Interestingly, a recent work by Granato et al. (2015) also finds too low SFRs in hydrodynamical simulations of proto-clusters, when comparing theoretical results with observational estimates by Clements et al. (2014). It should be noted that most if not all proto-clusters known at $z > 2$ are selected as overdense regions around radio galaxies. The elevated star formation rates measured for distant radio galaxies can only be sustained for a short period of time. Therefore, radio galaxy selected proto-clusters might be a special subset of proto-clusters with very high star formation rates, which could at least in part explain the mismatch between data and model predictions.

7 PASSIVE-GALAXY SEQUENCE

Passive elliptical-like galaxies represent a significant fraction of the local cluster galaxy population, particularly in the high-mass end. The spectroscopy of these galaxies becomes difficult at $z > 1$ (Cimatti et al. 2002; Daddi et al. 2004; Mo et al. 2010) not only because of the scarcity of such objects, but also because of the intrinsic difficulty in detecting them (usually they require a good continuum signal-to-noise ratio) and measuring their redshifts (see e.g. Gobat et al. 2011). However, recent observations demonstrate that the densest cores of most evolved cluster progenitors already host a (small) population of massive quiescent galaxies (see, e.g. Fassbender et al. 2014; Strazzullo et al. 2015, and references therein).

In this section we analyse in more details the galaxy population in our proto-cluster regions, and how it evolves as a function of cosmic time. In particular, we focus our attention on those galaxies that will become passive at $z = 0$. To this aim, we select all galaxies at redshift $z = 0$ that have $\log SSFR < -11$, which we consider as the threshold between passive and star-forming galaxies at any redshift. For this sample of galaxies, we select their progenitors in our proto-cluster regions and study when and how their star formation rate is suppressed.

We start by considering the location of all progenitors of passive galaxies today in the specific star formation rate-stellar mass plane. This is shown in Fig. 8 for four different redshifts. Progenitors are colour-coded according to their hierarchy (blue points and cyan lines are used for central galaxies and red points and lines for satellites). At high redshifts, 90 per cent of the progenitors are active, while the fraction of active galaxies decreases with decreasing redshift with 9 per cent of the central progenitors passive at $z \sim 0.8$, and 69 per cent of the satellites being passive at the same redshift. Moreover, Fig. 8 also shows that the most massive passive galaxies are centrals since $z \sim 2.2$. Observational studies are typically limited to the most massive passive

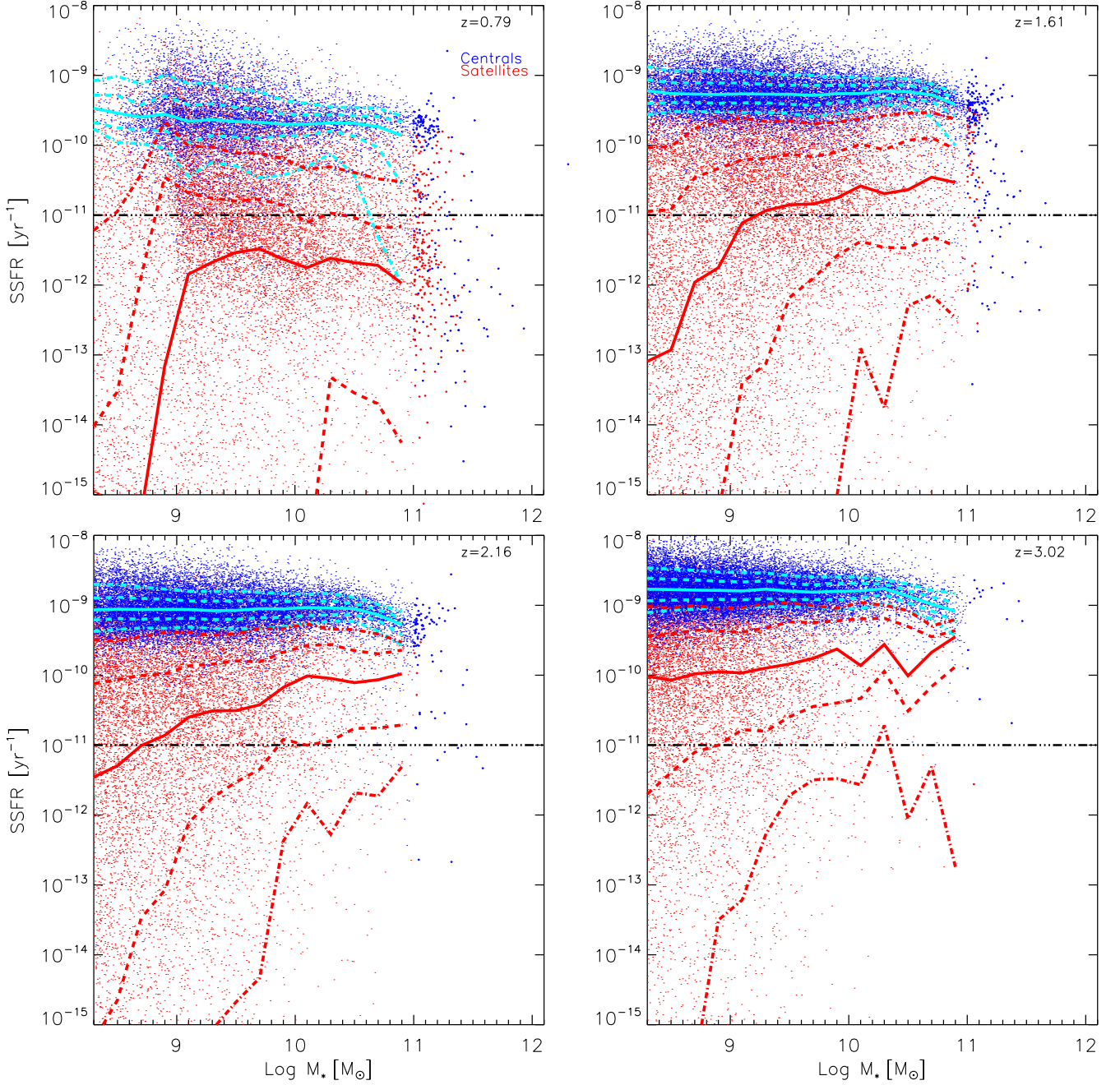


Figure 8. Specific star formation rate-stellar mass relation at redshifts $z = 0.79, 1.61, 2.16, 3.02$ (different panels) for progenitors that are central (blue) and satellite (red) of passive galaxies in clusters at $z = 0$. Solid lines represent medians, while dashed and dot-dashed lines represent the 30th-70th and 15th-85th percentiles, respectively, cyan for centrals and red for satellites. Larger symbols have been used for galaxies more massive than $10^{11} M_{\odot}$.

The black horizontal dash-dotted line represents our threshold in specific star formation rate that separates passive and active galaxies.

galaxies in proto-clusters, those with $M_* > 10^{10.5} M_{\odot}$. As we will discuss below, a large fraction of these galaxies in our model are quenched centrals, from AGN feedback. So, while the growth of the red-sequence at lower redshift is caused primarily by quenching of satellite galaxies, the passive galaxies that we can observe in distant clusters and in protoclusters are likely to be quenched by a different mechanism (AGN feedback).

In our model, galaxies that are accreted on larger structures (i.e. become satellites) are instantaneously stripped of

the hot gas reservoir that can fuel new material available for star formation through gas cooling. The combination of instantaneous hot gas stripping and relatively efficient supernova feedback adopted makes the transition from blue to red very short for satellite galaxies (Weinmann et al. 2006; Wang et al. 2007). It is therefore expected that most of the satellites in our models are passive. Fig. 9 shows the fraction of passive progenitors in the top panel and that of progenitors that are satellites in the bottom panel, as a function of the redshift of our proto-cluster regions. We have consid-

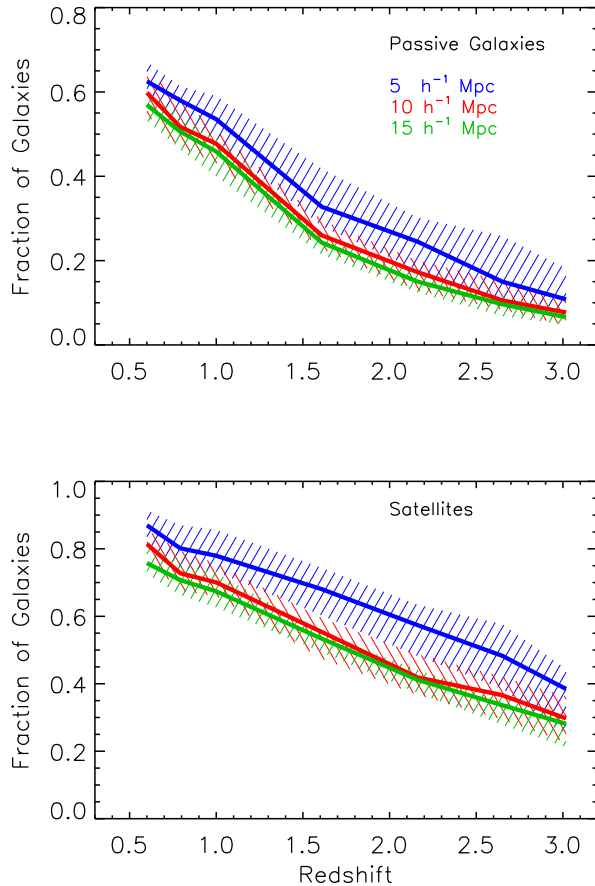


Figure 9. Fraction of passive galaxies (top panel) and satellites (bottom panel) within boxes of different sizes (different colours) centred around the CG, as a function of redshift. Solid lines represent the median value calculated on the 27 proto-cluster regions (22 for the largest box), while dashed areas represent the distribution between the 20th and 80th percentiles. The threshold in stellar mass is $M_* = 10^9 M_\odot$, but the trends shown do not depend on the particular threshold chosen.

ered in this case only progenitors with stellar mass larger than $10^9 M_\odot$ and residing in boxes with different size (different colours). Both fractions depend on the size of the box, and decrease with increasing size of the box because larger boxes capture more star forming progenitors, preferentially located at larger distances from the CG with respect to passive ones. At redshift $z \gtrsim 2$ the fraction of passive progenitors is not higher than 30 per cent, which confirms that the dominant population in proto-clusters is made up by star forming galaxies.

Both the fraction of satellite progenitors and that of passive ones increase at decreasing redshift, but the figure shows that the fraction of passive progenitors is smaller (less than half) than the fraction of satellites at high redshift, and increases faster towards lower redshift.

As highlighted above, the suppression of gas cooling makes satellite galaxies passive on relatively short time-scales, in the model. This is a well known problem pointed out by several authors (Weinmann et al. 2006; Font et al. 2008; Weinmann et al. 2010; Hirschmann et al. 2012). As shown by Figure 9, many satellites are still active at high- z .

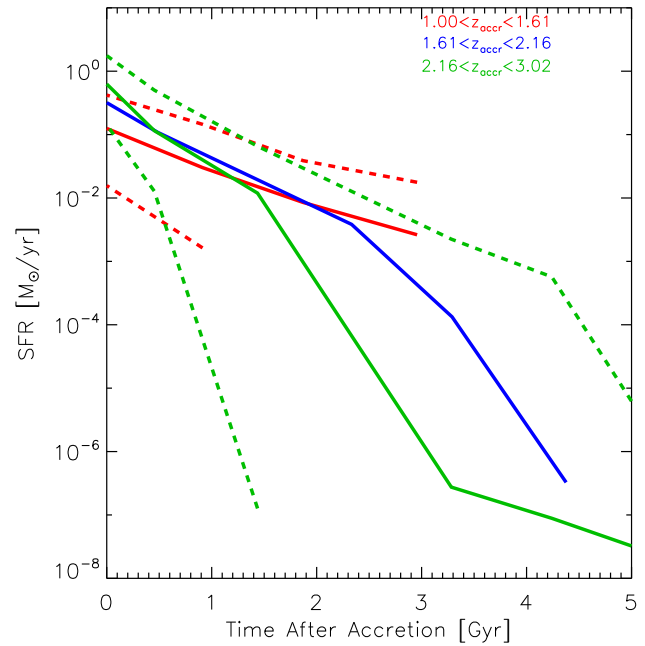


Figure 10. Star formation rate of progenitors of satellite galaxies with mass in the range $[10^9 - 10^{9.5}] M_\odot$ accreted at different redshifts, as shown in the legend, as a function of time elapsed since accretion. Solid lines represent the median value calculated on the 27 proto-cluster regions (22 for the largest box), while dashed areas represent the distribution between the 20th and 80th percentiles (the scatter corresponding to the blue line is comparable to that obtained for progenitors accreted at higher redshift, and is omitted to make the figure less crowded).

This is because they have been accreted very recently and the amount of cold gas available is still enough to keep them active.

In Figure 10 we show the star formation rate of progenitors of satellite galaxies with mass in the range $[10^9 - 10^{9.5}] M_\odot$ accreted at different times (red, blue and green lines for $1 < z_{\text{accr}} < 1.61$, $1.61 < z_{\text{accr}} < 2.16$ and $2.16 < z_{\text{accr}} < 3.02$, respectively), as a function of the time after accretion. This plot shows that progenitors accreted earlier (green line) have the tendency to be slightly more star forming than those accreted later (red line), at the time of accretion (although the scatter is very large). We find that this is driven by a higher cold gas fraction for galaxies accreted at higher redshift. In particular, we find that progenitors accreted in the range $2.16 < z_{\text{accr}} < 3.02$ have gas fraction (M_{cold}/M_*) larger by about 34 per cent than that of progenitors accreted in the range $1.61 < z_{\text{accr}} < 2.16$, and about twice that of progenitors accreted in the redshift range $1 < z_{\text{accr}} < 1.61$. Moreover, Figure 10 suggests that, at a given stellar mass, the quenching time-scale is shorter for galaxies accreted at high redshift (the green line is steeper than the red line), where galaxies tend to be less massive and to reside in lower halo mass and eject mass more efficiently. We have analysed galaxies having different values of stellar mass measured at $z=0$, and verified that the qualitative picture remains the same.

Figure 9 is suggesting that satellite galaxies are likely the major contributors in building-up the passive-sequence. In order to better quantify the relative contribution to the

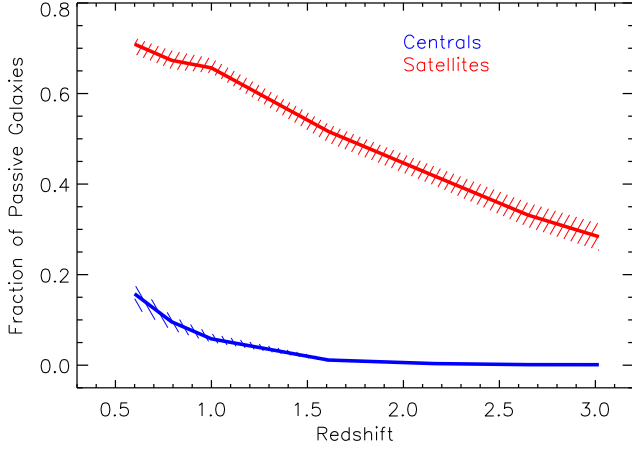


Figure 11. Fraction of passive satellites and centrals, progenitors of passive galaxies in clusters as a function of redshift. Solid lines represent the median value calculated on the 27 proto-cluster regions, while dashed areas represent the distribution between the 20th and 80th percentiles.

passive-sequence given by satellites and centrals, we plot in Figure 11 the fraction of passive satellites (red) and passive centrals (blue) that are progenitors of passive galaxies in clusters and stellar mass larger than $10^9 M_\odot$, as a function of time. Focusing on the redshift range of interest of proto-clusters ($z \gtrsim 2$), we find that most of the satellites are still active (as found above). Indeed, the fraction of passives is ~ 0.4 at $z = 2$, and it increases with decreasing redshift, reaching 0.7 at $z \sim 0.6$. Different is the picture for centrals: they are almost all active down to $z \sim 1$ and only 15 per cent of them are passive at $z \sim 0.6$.

A small, but not-negligible, fraction (around 15 per cent at $z \sim 0.6$) of central galaxies that are progenitors of passive galaxies in clusters start to be quenched at $z \sim 1.3$. We addressed this point and found that many are intermediate-mass galaxies (30 per cent with $M_* \gtrsim 10^{10.4} M_\odot$ and a median value of $M_* \gtrsim 10^{10.2} M_\odot$ at $z \sim 0.6$). The main responsible for their quenching is found to be a strong AGN feedback, that prevents cooling of hot gas (at any stellar mass) which would replenish the cold reservoir. Nevertheless, we find that around 10 per cent of these galaxies experience a burst of star formation between $z = 1$ and $z = 1.5$. This is due to a rapid cooling of hot gas (coming from newly accreted satellites), that enhances star formation. In a few cases, the burst is also driven by mergers.

The analysis done in this section points out that galaxies in proto-clusters are star forming objects at any time, and the passive-sequence of galaxies emerges at around redshift $z \sim 1$. Centrals are star forming down to low redshift, but a small fraction of them are quenched by AGN feedback, while satellites are quenched by stripping of their hot gas reservoir at the time of accretion. The time during which they keep forming stars depends on the amount of cold gas available at accretion.

8 CONCLUSIONS

We have analysed a sample of 27 proto-cluster regions extracted from a set of N-body simulations, that become mas-

sive clusters, with $M \sim 10^{15} M_\odot$, at $z = 0$. These regions have been built by considering all progenitors of $z = 0$ galaxies within the virial radius R_{200} of the clusters into which these objects will evolve.

The case study shows that progenitors of galaxies in massive galaxy clusters distribute in a very large region at high redshift. This region is dominated by central galaxies at high redshift. Their number decreases with time because many become satellites, clustering around the central object. We find that the velocity dispersion of galaxies increases with cosmic time, in good agreement with observations, and that of satellites increases faster, in line with a picture where galaxies grow in mass as centrals and then join the densest regions as satellites.

In agreement with estimates based on the spatial distribution of galaxies around the Spiderweb Galaxy (Hatch et al. 2009), we find that 95 per cent of the satellites within a radius of $150 kpc$ from the central object at redshift $z \sim 2$ will merge with it by $z = 0$. This implies that mergers are important in building-up the central object and for the overall evolution of such regions.

Our analysis highlights that proto-clusters are very extended objects. Indeed, we find that at most 60 per cent of progenitors are located within a box of $15 h^{-1} Mpc$ size centred on the central galaxy of the proto-cluster, at redshift higher than ~ 1.5 . The percentage decreases drastically in smaller boxes, to at most 20 per cent for $5 h^{-1} Mpc$ apertures. This demonstrates that one has to consider fairly large regions, having comoving sizes larger than $15 h^{-1} Mpc$, in order to trace the distribution of a large fraction of the progenitors of galaxies belonging to local clusters. Moreover, we find a shift between the geometrical centre of the proto-cluster and the position of the central objects (that observers usually take as the centre of the proto-cluster), that affects the fraction of progenitors in the box. This suggests that attention must be paid when comparing observations with model predictions when the size of the proto-cluster region is relatively small.

We find that the fraction of outliers, i.e. those galaxies that are not progenitors of any cluster galaxy at $z = 0$, is dependent on the galaxy stellar mass and on redshift, and does not strongly depend on the size of the box up to 15 comoving Mpc. On average, we find that about 30 per cent of galaxies with stellar mass smaller than $\sim 10^{10} M_\odot$, and about 20 per cent of galaxies with larger stellar masses, are outliers in proto-cluster regions at $z \sim 3$. Slightly smaller fractions are found at lower redshift and/or considering only progenitors of galaxies within the virial radius (instead of $2 \cdot R_{200}$). It is virtually impossible to distinguish outliers from actual progenitors just by looking at their properties.

We have focused on progenitors of passive-sequence galaxies at $z = 0$, and studied when the passive-sequence emerges. At high redshift ($z \sim 3$) we find that 90 per cent of progenitors are still active, confirming that star forming galaxies are the dominant population in proto-clusters. Moreover, central and satellite galaxies show a different evolution with time. We find that satellites are the main contributors in building-up the passive sequence, but many of them are still active at high redshift (see Fig. 11) and their quenching is regulated by the amount of cold gas available at the time of accretion. Nevertheless, the timescale for quenching depends on the time of accretion, being shorter

for progenitors accreted at higher redshifts. Central galaxies contribute little and only at lower redshift. Only a small fraction of them start to be quenched after $z \sim 1.3$, and a strong AGN feedback is the responsible for their quenching, independently on the galaxy stellar mass.

Galaxies in proto-clusters are actively star forming, more intensively at increasing redshift. Nevertheless, if we consider a minimum dust correction, our model predicts proto-cluster regions that are systematically less star forming than those observed, and tend to be even less star forming than observed if we take into account apertures larger than 1 Mpc. Although large uncertainties exist in the data, the lowest observationally measured star formation rates quoted in this paper are still significantly higher than the highest predicted by our model.

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